Equations Consolidation

1. Solve:

(a)
$$4x - 2 = 3x + 8$$
.

(b)
$$3 - 5x = 2x - 1$$
. $x = \frac{4}{7}$

(c)
$$2x - 7 = 5x - 7$$
.

2. Solve:

(a)
$$2(x+3) + 4(2x+1) = 1$$
. $x = -\frac{9}{10}$

(b)
$$3(2x-1)-2(x+4)=2x-7$$
.

(c)
$$2x - 3(8 - x) = 7(2 - 5x)$$
.

(d)
$$2 - (2x - 19) = 2(7 - 8x)$$
.

(e)
$$(x-3)(x-7) = (x+1)(x-2)$$
.

(f)
$$(2x+1)(5-x) = 6 - (3-x)(7-2x)$$
.

3. In the equation x - a = b the solution is x = b + a. Therefore in the following equations attempt to solve them by isolating the x.

(a)
$$ax - b = c$$
.

(b)
$$ax + b = b$$
.

(c)
$$\frac{x}{a} + b = c$$
.

(d)
$$a = \frac{b}{x}$$
.

(e)
$$\frac{ax}{b+c} = a$$
.

(f)
$$ax + d = 3x - 2$$
. $x = \frac{2+d}{3-a}$

(g)
$$\frac{ax}{bx+c} = d$$
. $x = \frac{cd}{a-bd}$

(h)
$$\frac{x-e}{x+ax-f} = d.$$

$$x = \frac{e-df}{1-d-ad}$$

(i)
$$(ax+2)(x-3) = a(x-3)(x-k)$$
. $x = \frac{3ak+d}{2+ak}$

4. Solve:

(a)
$$\frac{x}{3} + 7 = \frac{2x}{4}$$
.

(b)
$$\frac{2x+1}{4} + \frac{3x-1}{5} = 1.$$
 $x = \frac{19}{22}$

(c)
$$\frac{3x-2}{2} - \frac{2-x}{5} = \frac{x+1}{10}$$
. $x = \frac{15}{16}$

(d)
$$\frac{2(x+1)}{3} - 2 = \frac{4x-1}{7} + \frac{2}{3}$$
.

(e)
$$\frac{2x+5}{x} = 3\frac{2}{3}$$
.

5. Solve the following simultaneous equations:

(a)
$$x + y = 5$$
 $x - y = 1$ $(x, y) = (3, 2)$

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(b)
$$2x + y = 7$$
 $x - y = 5$ $(x, y) = (4, -1)$

$$x - y = 5$$

$$2x + y = 5$$

$$4x + 3y = 14$$
(d)
$$x + 2y = 6$$

$$3x - 2y = 0$$

$$2x + 3y = 42$$
(e)
$$2x + 3y = 42$$

$$3x - 4y = -5$$

$$(x, y) = (\frac{3}{2}, \frac{9}{4})$$

$$(x, y) = (9, 8)$$

(d)
$$x + 2y = 6$$

$$3x - 2y = 0$$

$$(x, y) = \left(\frac{3}{2}, \frac{9}{4}\right)$$

(e)
$$2x + 3y = 42 3x - 4y = -5$$

$$(x, y) = (9, 8)$$

6. A couple of slightly more challenging questions to get you thinking...

(a)
$$\frac{2x + \frac{2x-1}{3}}{3} + 2x - 3 = 1.$$
 $x = \frac{37}{26}$

(b)
$$\frac{x+2y}{5} + \frac{5x-2y}{2} = \frac{3}{2}.$$

$$(x,y) = (1,2)$$

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